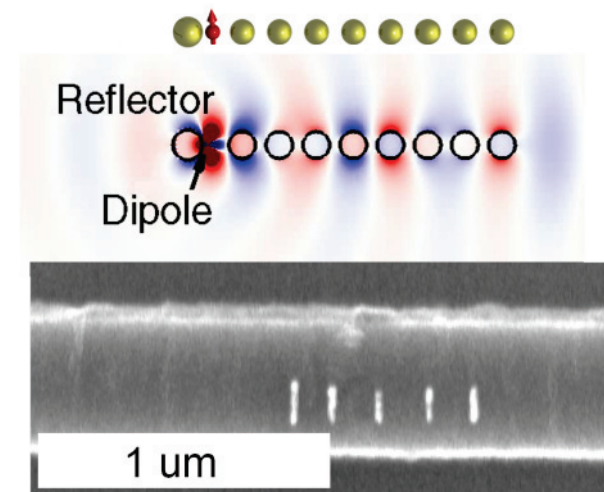
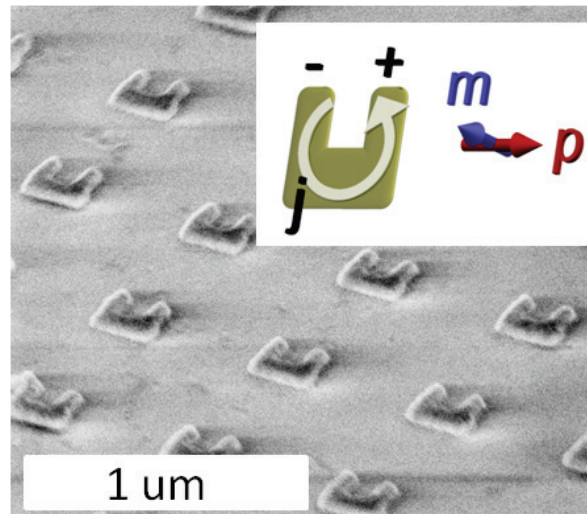


# Controlling single photons and single molecules with nano-antennas

Ivana Sersic  
Martin Frimmer  
Andrej Kwadrin  
Abbas Mohtashami  
Felipe Bernal  
Lutz Langguth  
Hinke Schokker  
Per Lunnemann




Femius Koenderink

Center for Nanophotonics  
FOM Institute AMOLF, Amsterdam  
[www.amolf.nl](http://www.amolf.nl)



# Single photons from single emitters



*photon*

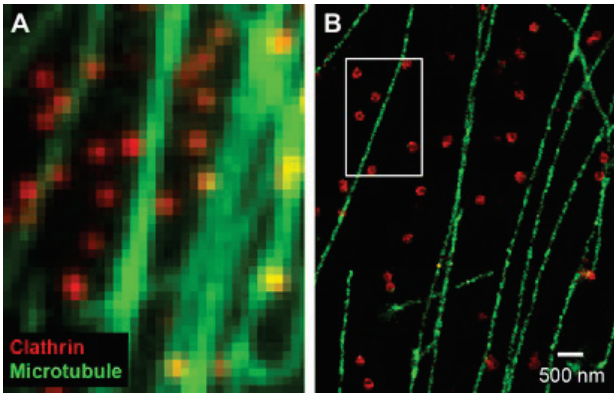
*photon*

*Single emitter*  
*Quantum dot, molecule*

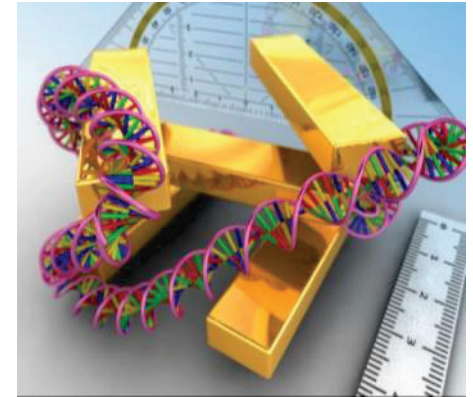
Challenges: (1) Surely catching each photon in a single beam  
(2) Surely absorbing each photon from a beam

Addressing and seeing single molecules *with unit efficiency*

# Motivation



Bates & Zhuang [PALM, STORM]



Liu & Alivisatos

**Optical microscopy**  
**Below  $\lambda/2$  limit**

Single molecules  
Information from  
fluctuations

**Single photon sources**  
**Quantum information**  
**Quantum communication**

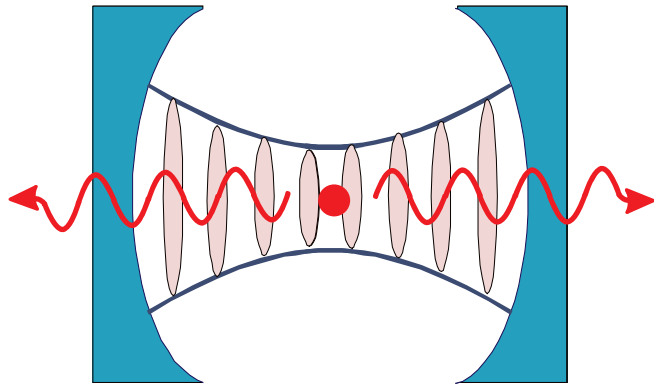
Quantum information  
in 1 photon can  
**not** be eavesdropped

**Spectroscopy of  
molecules**

Distance ruler,  
vibrations  
THz, IR and VIS

# Enhancing photon-emitter interaction

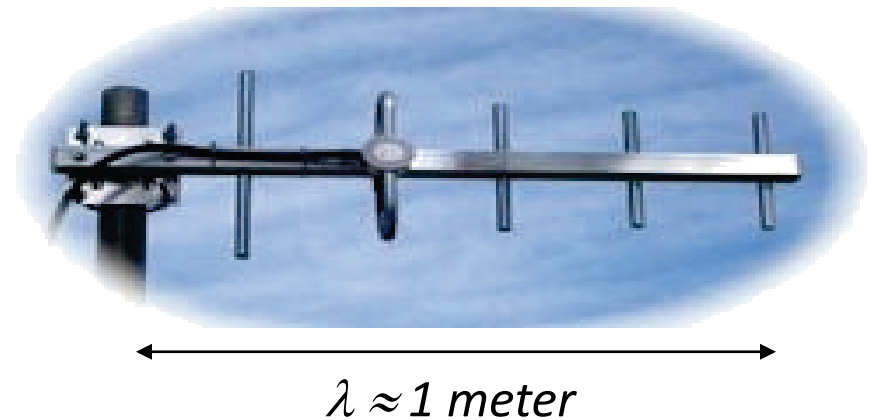
## Cavity resonances



Enhanced interaction time  $\propto Q$   
Enhanced  $|E|^2$  per photon  $\propto 1/V$

Limit on  $V > (\lambda/2)^3$   
Hence  $Q > 10^4$

## Antennas

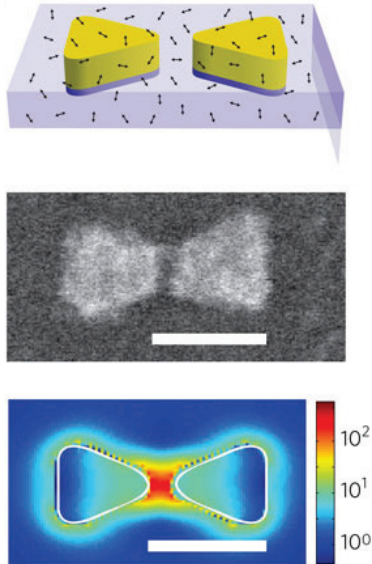


Very broadband:  $Q \approx 5$   
Strongly scattering, open system

Strong local field due to metal  
 $V \approx (\lambda/50)^3$

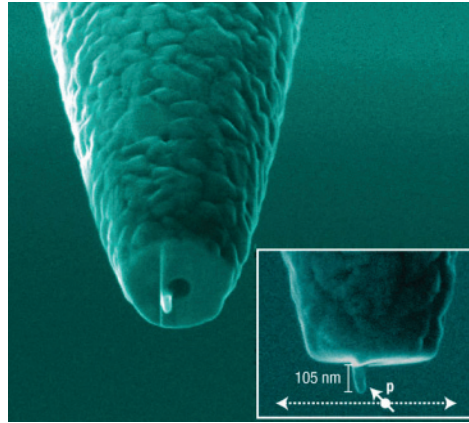
# Famous reported optical antennas

'Bow-tie' antenna



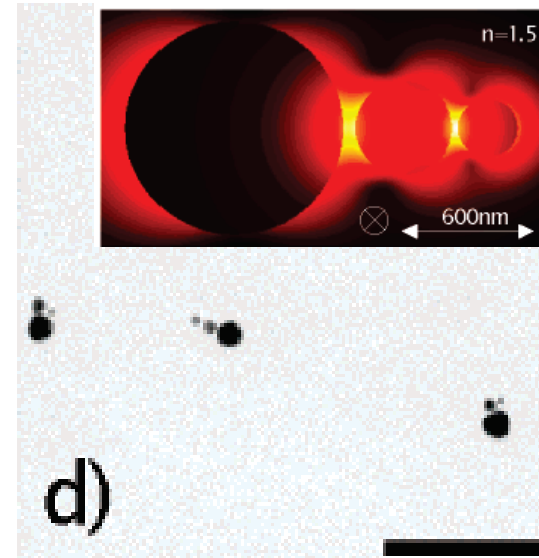
W. E. Moerner 2009  
Nature Photonics

' $\lambda/4$ ' antenna

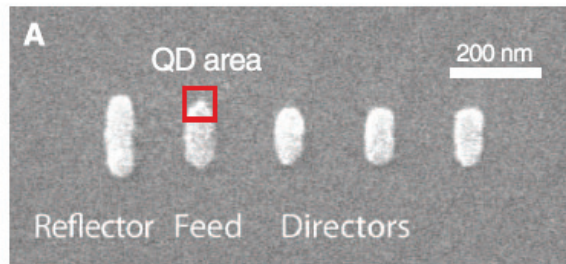


Van Hulst 2008  
Nature Photonics

Self-similar trimer



Bidault & Polman  
2009, JACS



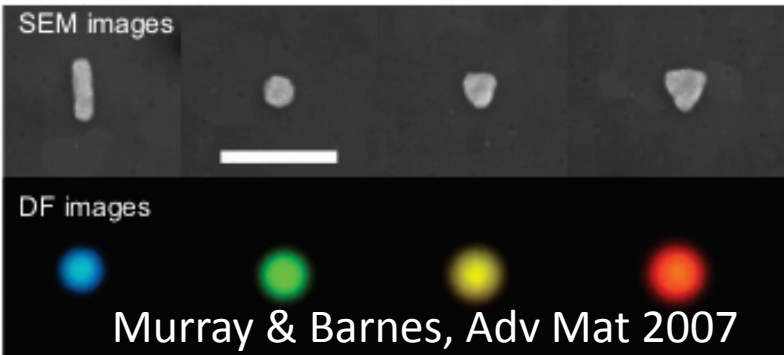
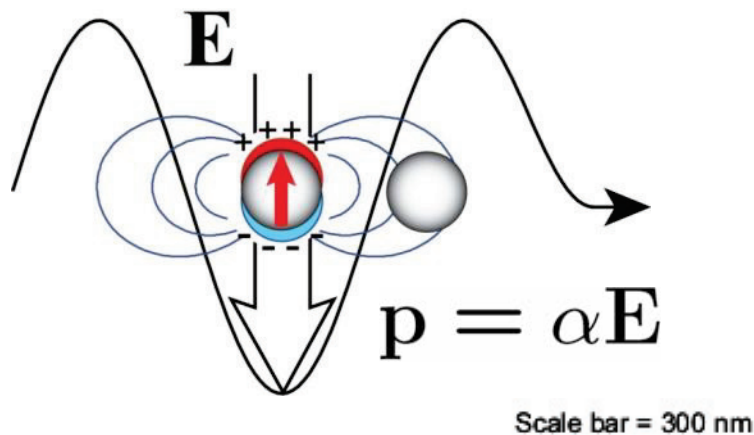
Yagi-Uda antenna

Van Hulst/Quidant 2010  
Nature Photonics

E-beam lithography  
Focused Ion Beam milling  
DNA-aided selfassembly

# Scattering resonance

## Plasmon resonance



Circa  $10^3$ - $10^4$  free electrons

Incident field separates  $e^-$  from ionic backbone

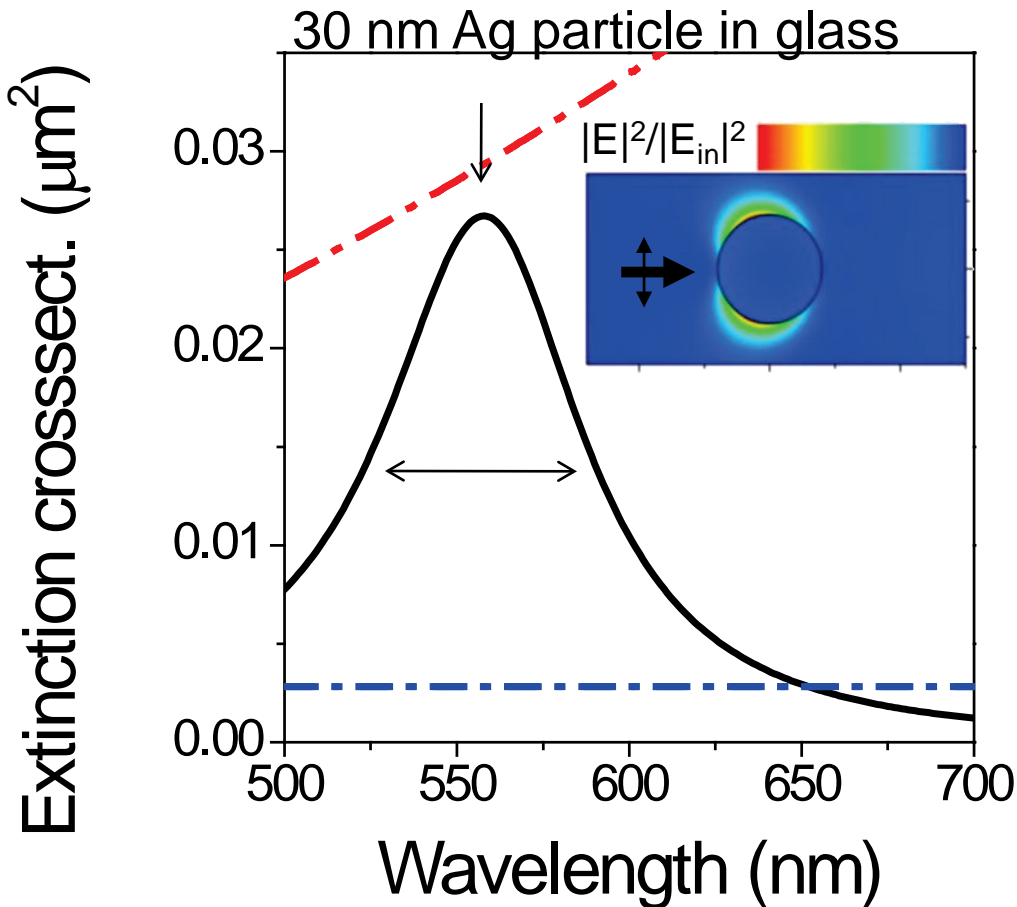
Linear restoring force implies a resonance

Resonant dipole scatterers

$\lambda \sim 300$ - $1000$  nm,  $Q \sim 5$ - $30$



# General properties

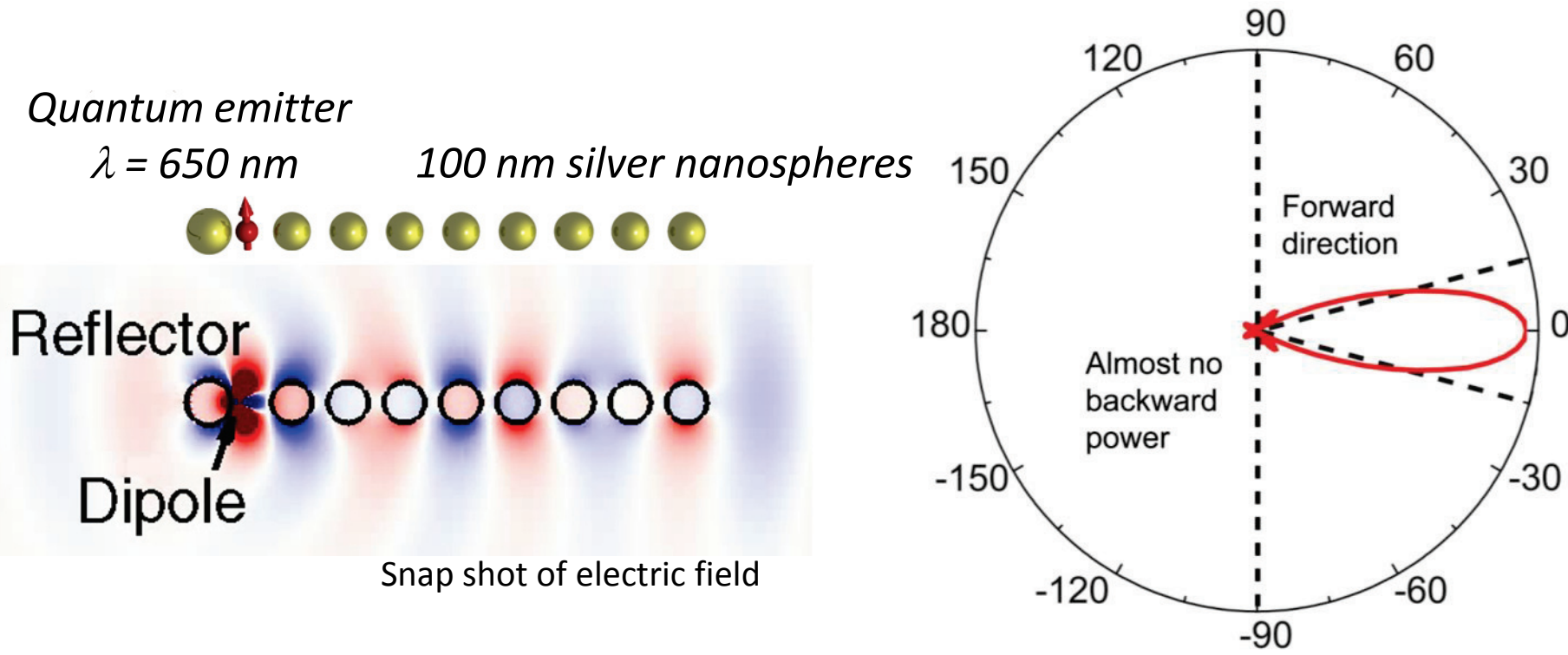


- Color tunable in visible
- Cross section  $\sim 10 \times \pi r^2$
- Strong dipolar near field
- $Q \sim 5$  means 95% of loss is radiation into free space
- $\sigma$  and  $\alpha$  at upper bound:

*unitary limit*  
*(Chu limit)*  $\sigma \approx \frac{3}{2\pi} \lambda^2$

***Plasmon particle is a solid state 'strongest point-scatterer'***

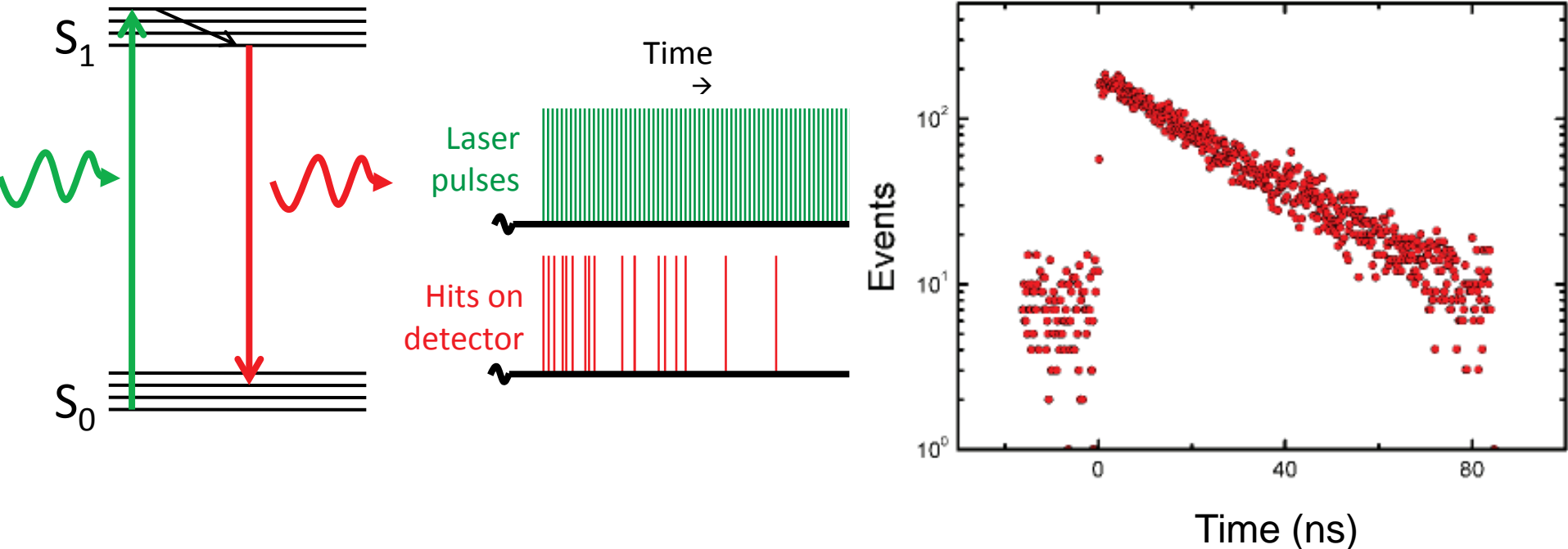
# Yagi-Uda



- Far-field: photon with 90% probability in a narrow beam
- Broadband ( $> 300 \text{ nm}$  bandwidth in the visible)
- 90% chance that the photon is not lost to heat



# Single quantum emitter



- After one excitation, emits just one quantum of light
- Probabilistic timing of *when* emission occurs
- Spatial and temporal coherence of single photon wavepackets
- No such thing as setting up multiple *coherent* active elements

# Fermi's Golden Rule



- 1) Dipole antenna
- 2) Ground plane

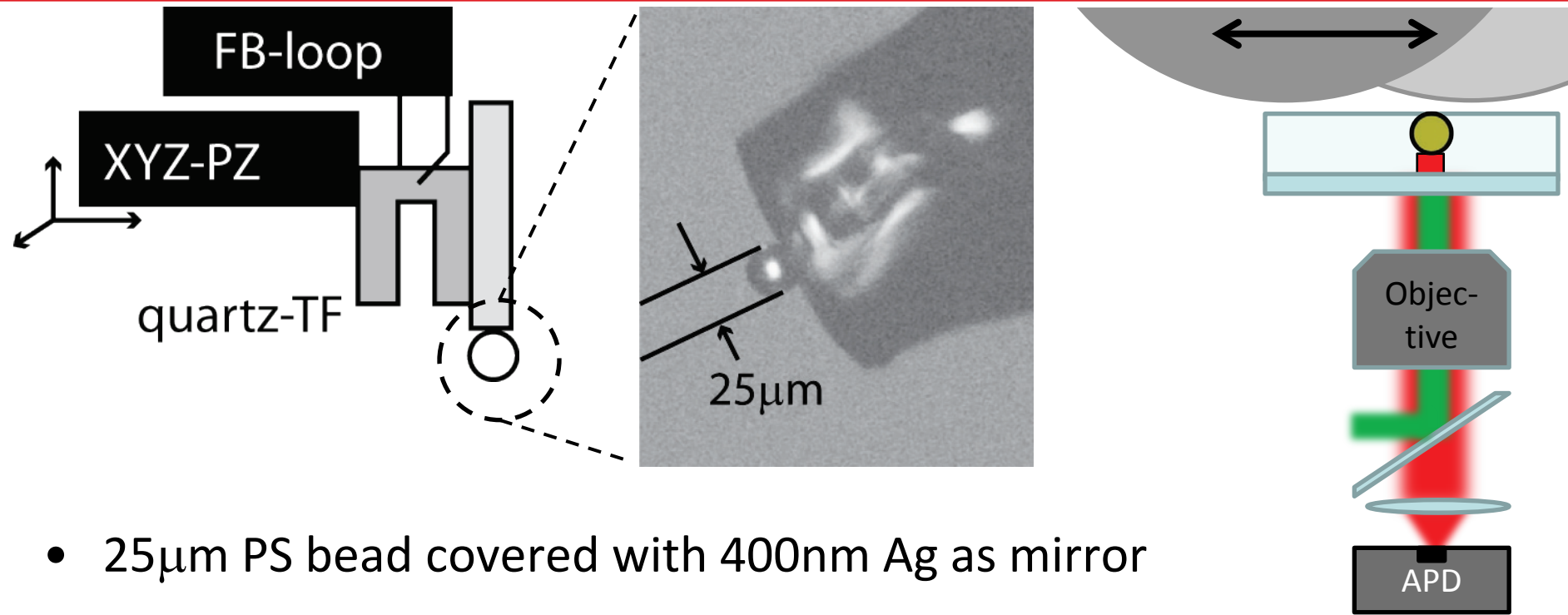
Optics:

“Drexhage experiment”

Emitter in front of mirror

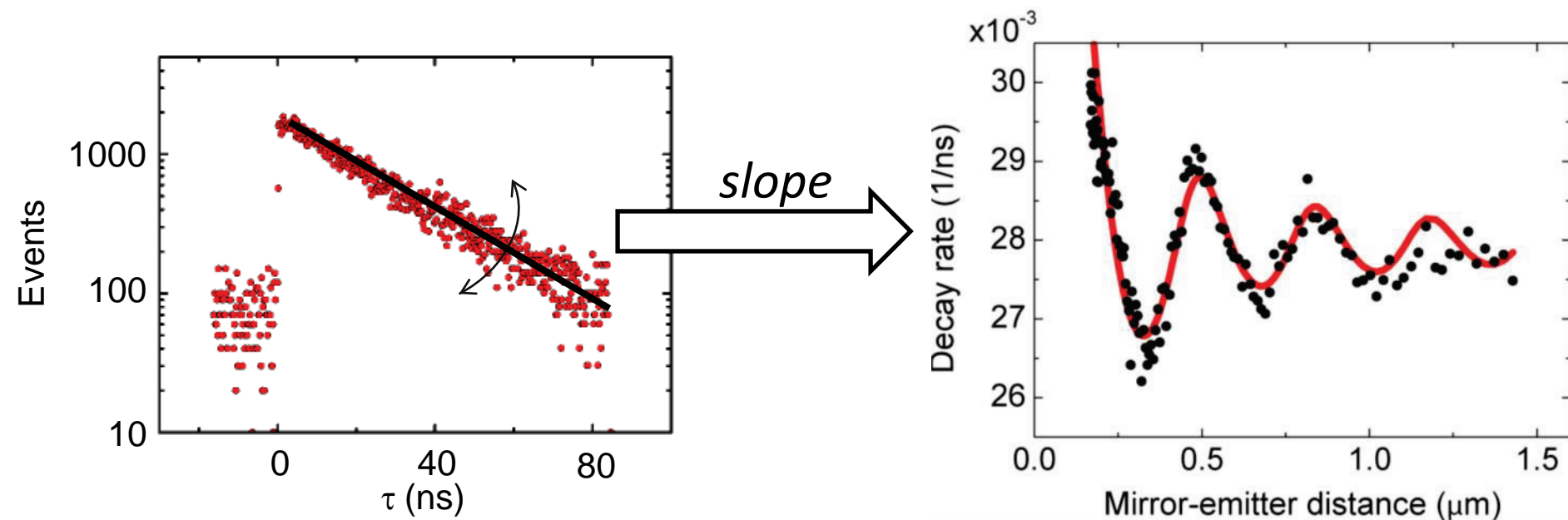
(Drexhage, 1968)

# Scanning mirror 'Drexhage experiment'



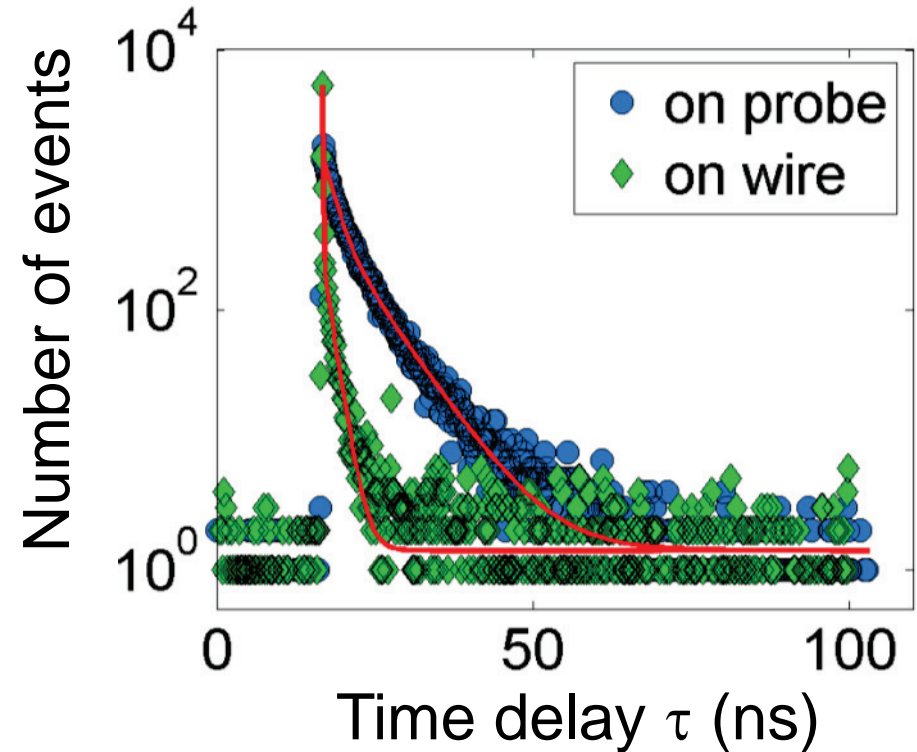
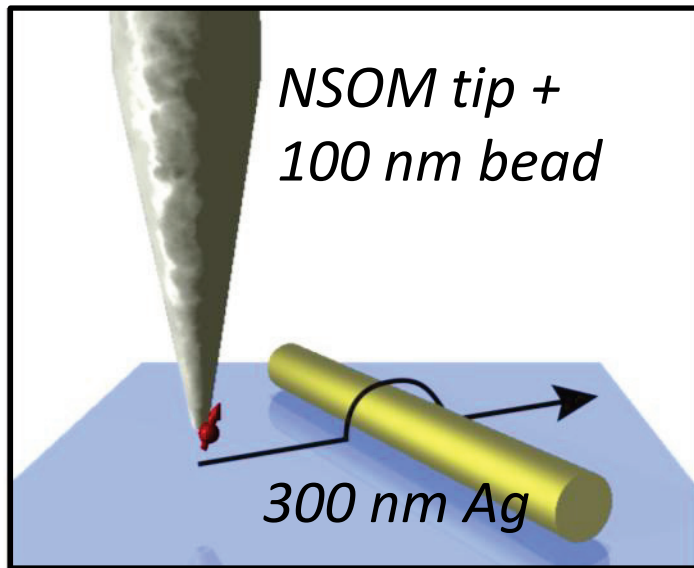
- 25 μm PS bead covered with 400nm Ag as mirror
- PS bead glued to cleaved fiber
- Lateral scanning in shear force varies emitter-mirror distance

# Calibration example – single NV center



- *Single* NV center in a 100 nm nanodiamond (MicroDiamant AG)
- Decay rate varies with distance to the mirror
  - radiative decay rate  $\Leftrightarrow$  radiative impedance
  - nonradiative decay rate  $\Leftrightarrow$  Ohmic resistance

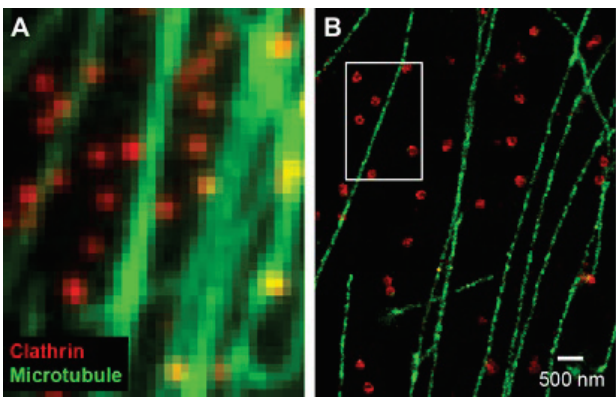
# Scanning LDOS microscope



Reversible control of light-matter coupling for *any* nano-structure

Nanoscale imaging LDOS changes in Fermi's Golden Rule

# Motivation



Bates & Zhuang [PALM, STORM]

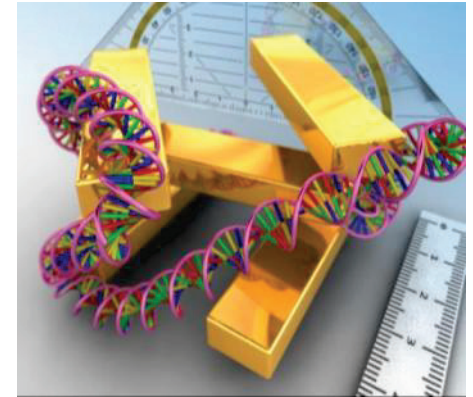
**Optical microscopy**  
Below  $\lambda/2$  limit

Single molecules  
Information from  
fluctuations



**Single photon sources**  
**Quantum information**  
**Quantum communication**

Quantum information  
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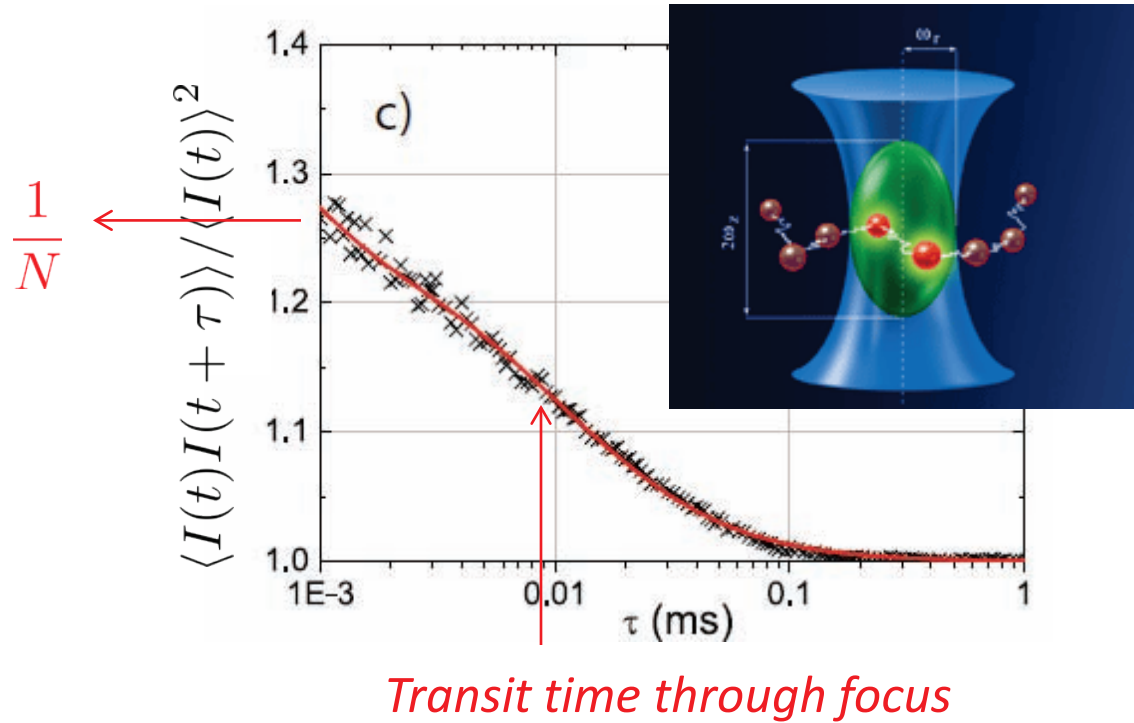
Liu & Alivisatos

**Spectroscopy of  
molecules**

Distance ruler  
Vibrations  
THz, IR and VIS



# Microscopy & antennas

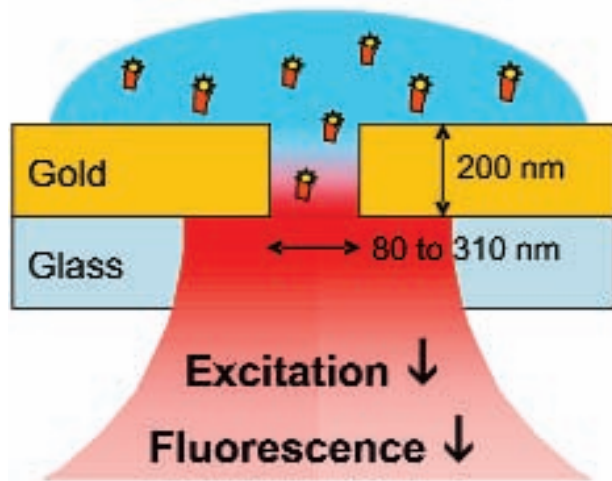


“Fluorescence correlation spectroscopy”

Photon correlations reveal density and diffusion constant of an analyte

Problems: requires  $< 1$  molecule per focal volume

# Microscopy & antennas



A single nano-aperture  
confines  
geometrically for FCS

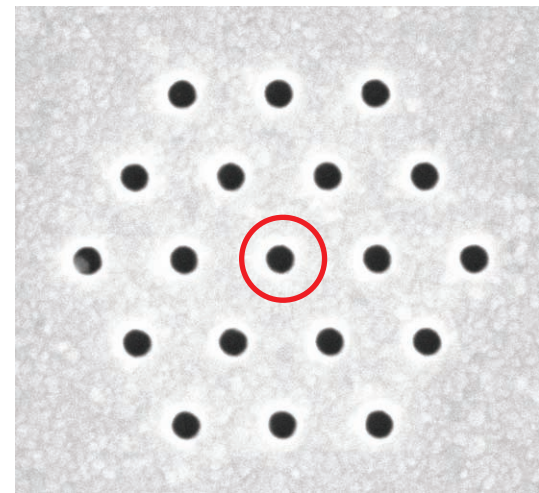
Plasmonic enhancements  
increase count rates  
and brightness

“Fluorescence  
Photometry”  
Pioneered by  
Levene et al. [2003]  
Wenger et al. [2005]

analyte

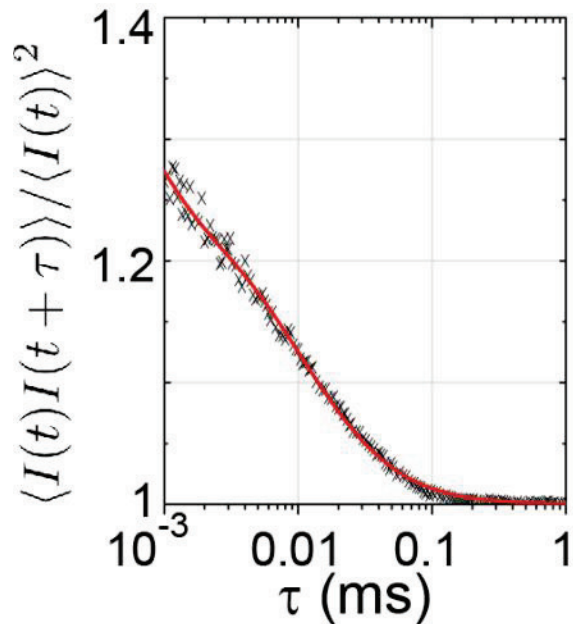
Problems: requires  $< 1$  molecule per focal volume

# Phased array



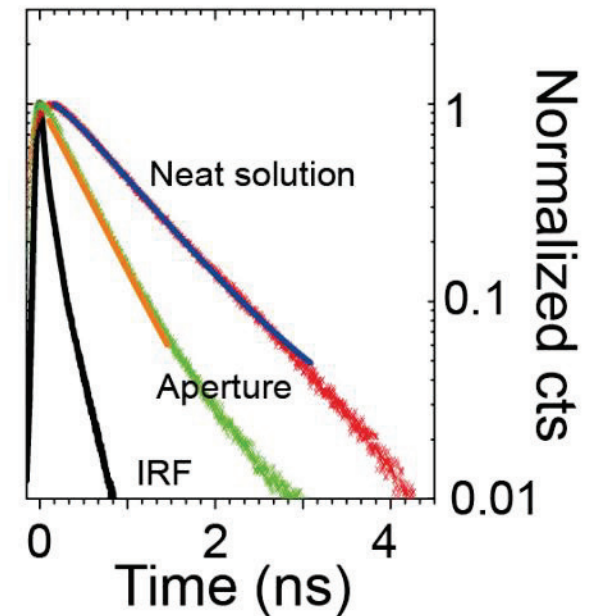
140 nm holes/150 nm  
Au film/440 nm pitch

We only pump molecules  
in the central hole



FCS correlation 1.3  
3 molecules/focus

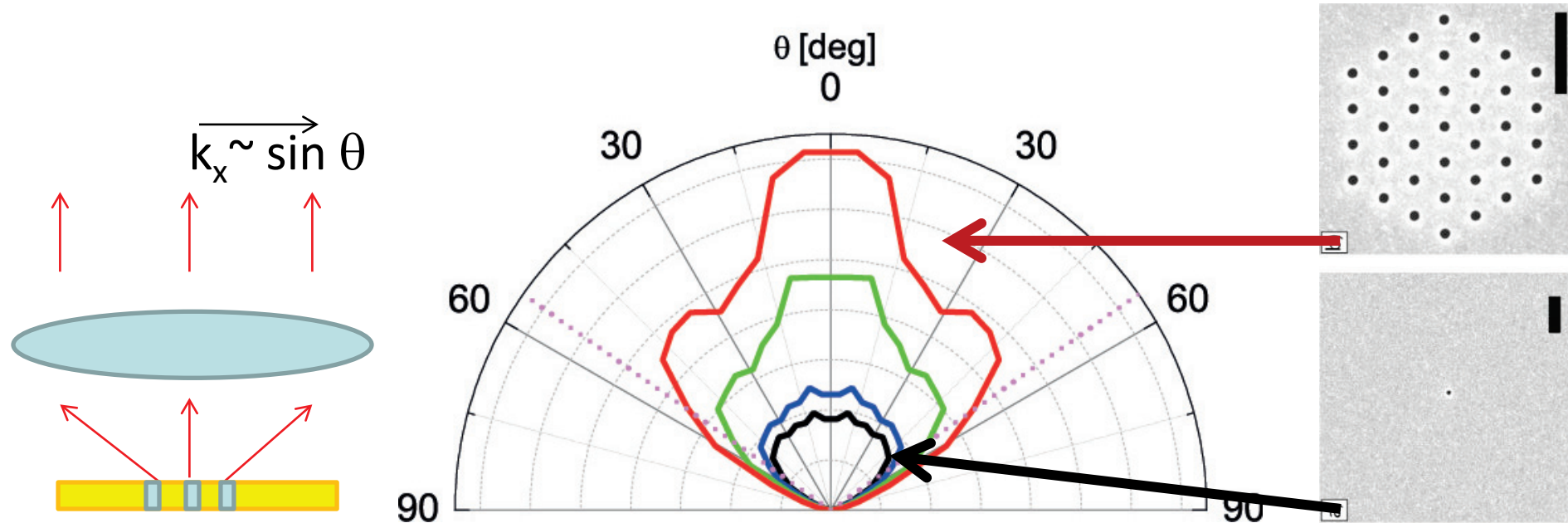
$$V \sim \lambda^3/20$$



Fluorescence  
lifetime

Circa 2-fold  
enhanced

# Fourier images – angular distribution

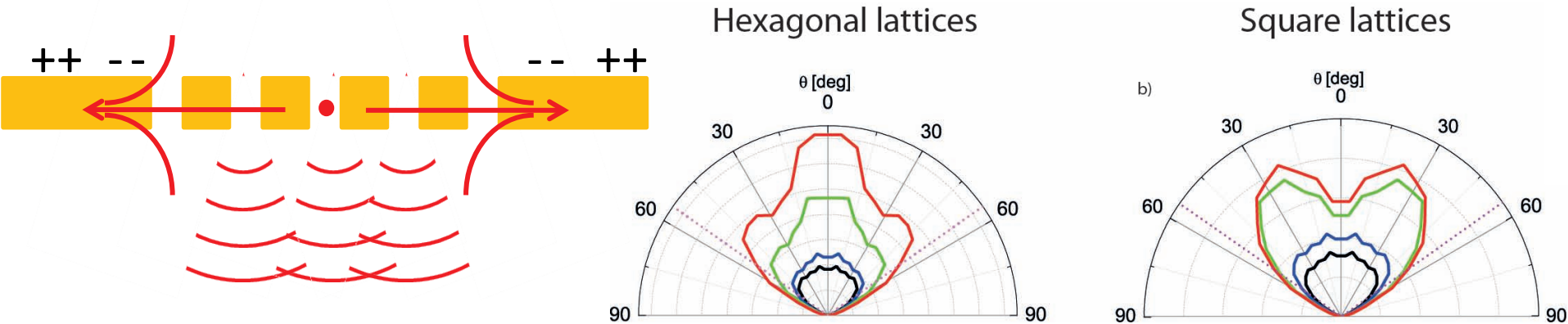


Emission *only* comes from the central hole

Yet, enhanced directivity and total strength (4 to 5 times)

*Plasmonic-crystal band edge phased array antenna*

# Phased array physics



The gold film supports a surface plasmon guided mode  $[k_{SPP}]$   
Direct photon + amplitude scattered from each hole with phase  $e^{ik_{SPP}r}$

Radiation pattern can be controlled via lattice parameter  
Around 2nd order plasmon diffraction (near dispersion band edge)

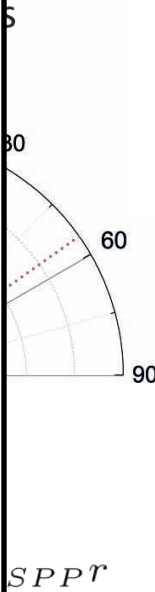
# Phased array physics

++

Plasmon phased arrays improve single molecule brightness and directivity, as well as emission rate

Also:

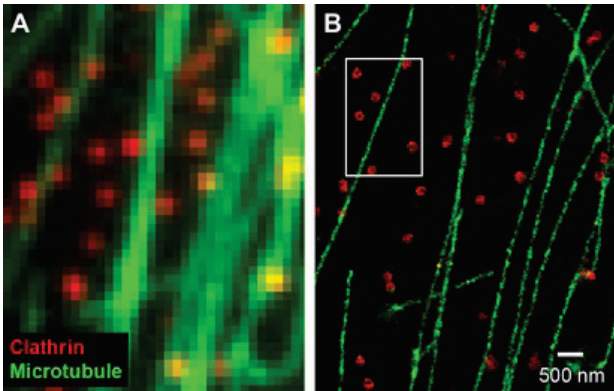
- Yagi Uda + single quantum dot [Curto et al., Science 2010]
- 1D chain antenna receiver [de Waele et al., Nano Lett. 2007]
- 2D infinite lattices to improve LED extraction  
[G. Vecchi et al., PRL 2007, LED's]
- Bull's eyes around holes [Wenger et al., Nano Lett. 2012, FCS]



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Radi  
Arou



# Motivation



Bates & Zhuang [PALM, STORM]

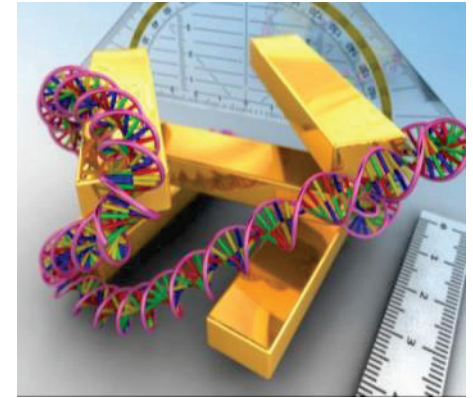
**Optical microscopy**  
Below  $\lambda/2$  limit

Single molecules  
Information from  
fluctuations



**Single photon sources**  
**Quantum information**  
**Quantum communication**

Quantum information  
in 1 photon can  
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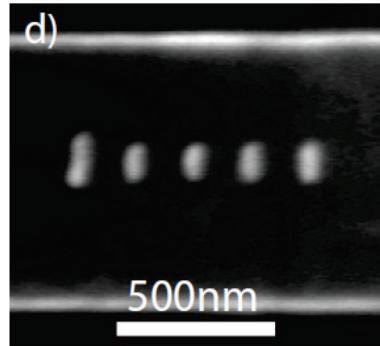


Liu & Alivisatos

**Spectroscopy of  
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Distance ruler  
Vibrations  
THz, IR and VIS

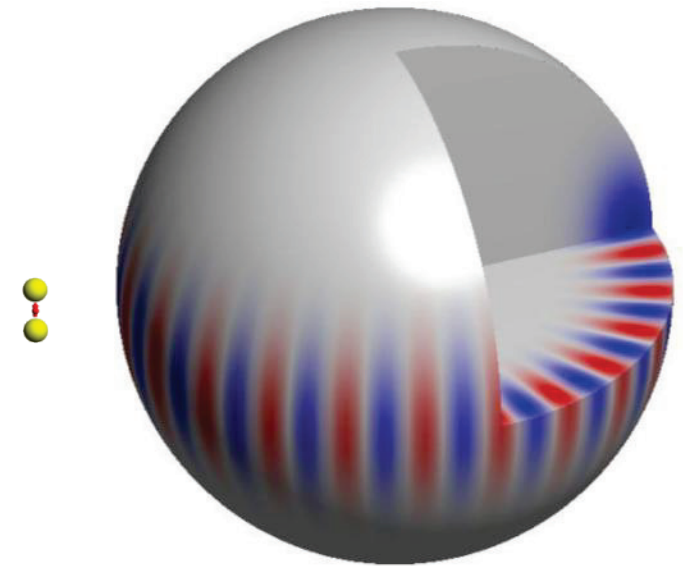
# Complex world



Yagi – Uda *ON* a waveguide

Full scattering study:

Bernal, ACS Nano **6** 10156 (2012)

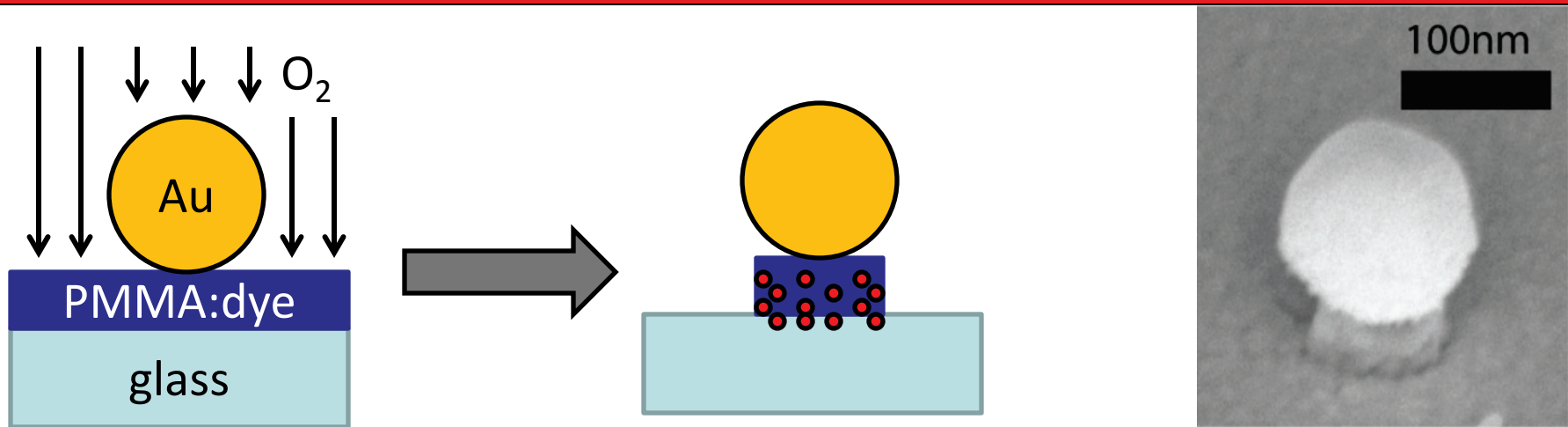


Cavity-assisted plasmonics

Fundamental question: antenna in a nontrivial mode bath ?

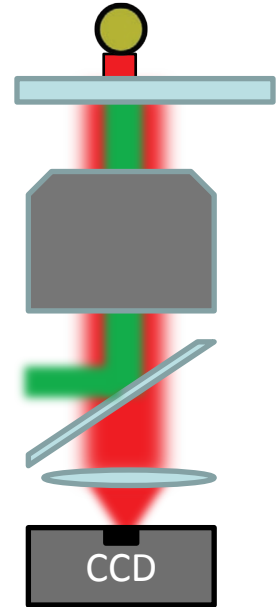
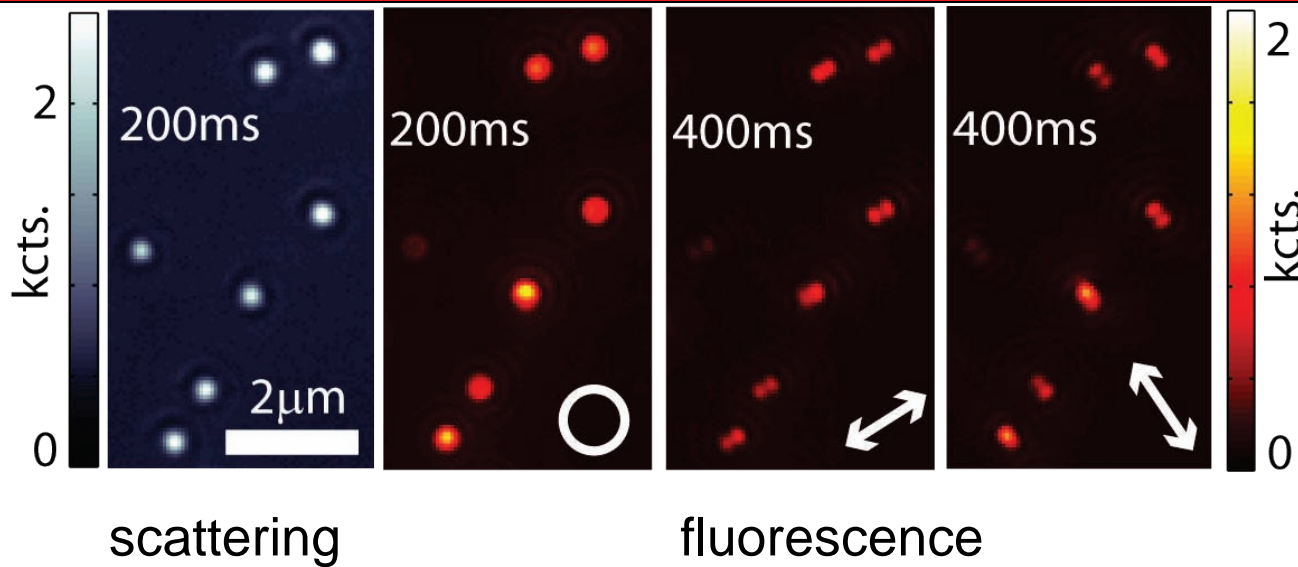
Key parameter: decay rate enhancement (Purcell factor)

# Simplest possible “dipole” antenna



- Au colloid on dye doped PMMA layer on glass
- O<sub>2</sub> plasma removes dyes layer except under colloid

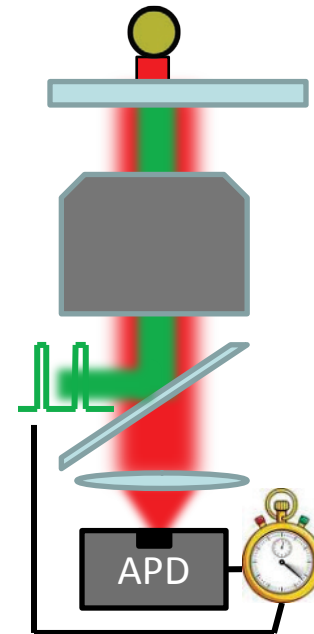
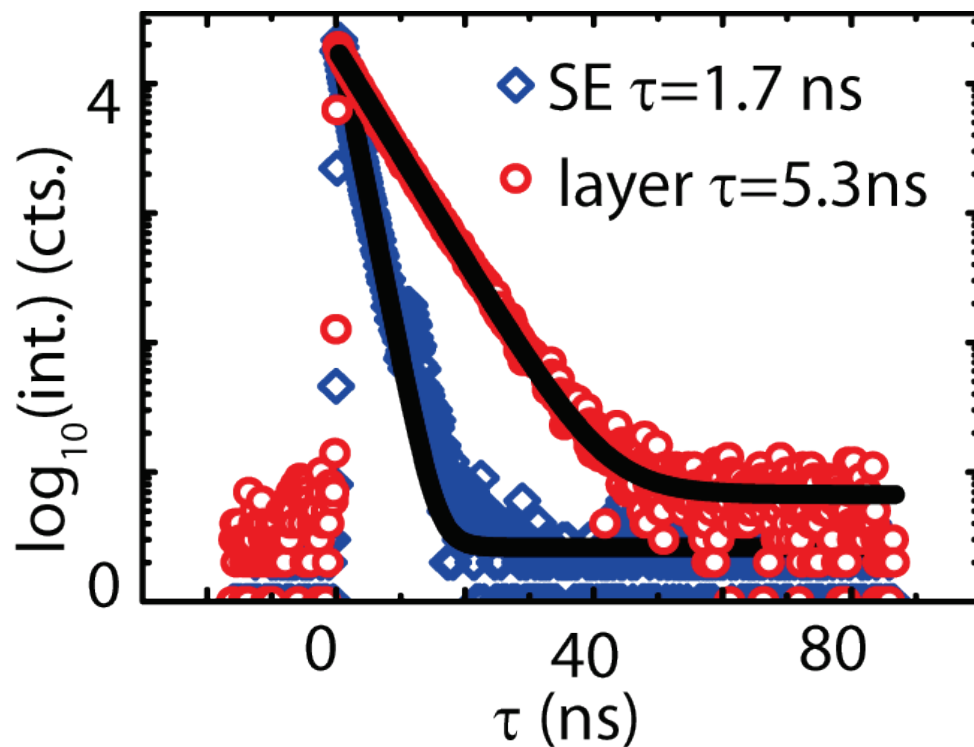
# Superemitter - polarization



- Unpolarized: donut-shaped image
- Polarization analyzed: double lobes

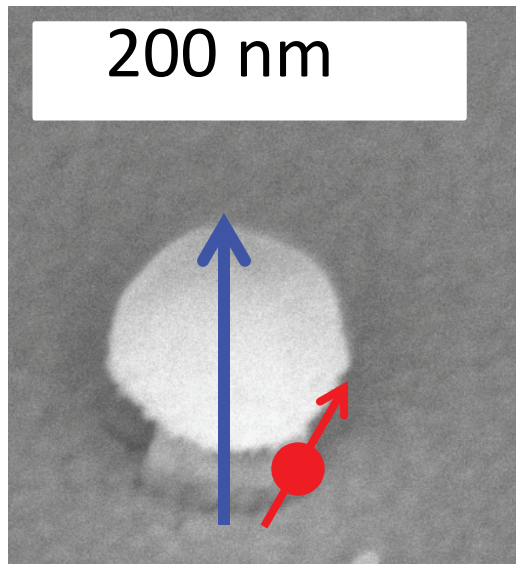
→ Superemitter dipole moment along optical axis

# Superemitter - lifetime



- TCSPC-FLIM measurement (pump 532 nm, 10 MHz)
- Antenna rate enhancement ca. 3x compared to bare dye layer

# Zero order idea



$$\mathbf{P} = \mathbf{p}_0 \left[ 1 + \frac{\alpha(\omega)}{r^3} \right]$$

Antenna dominates molecular dipole

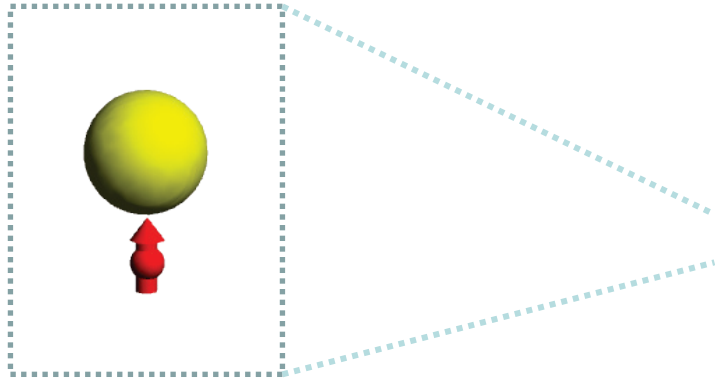
Classically, the radiated power of a dipole scales with  $|\mathbf{p}|^2$

$$\text{Decay rate change} = 1 / Z_{\text{antenna}} \sim \left| \alpha(\omega) / r^3 \right|^2$$



# Hybrid systems – lumping LDOS

## System 1: Super-emitter



Polarizable nanoparticle  
in near-field of molecule

## System 2: ground plane

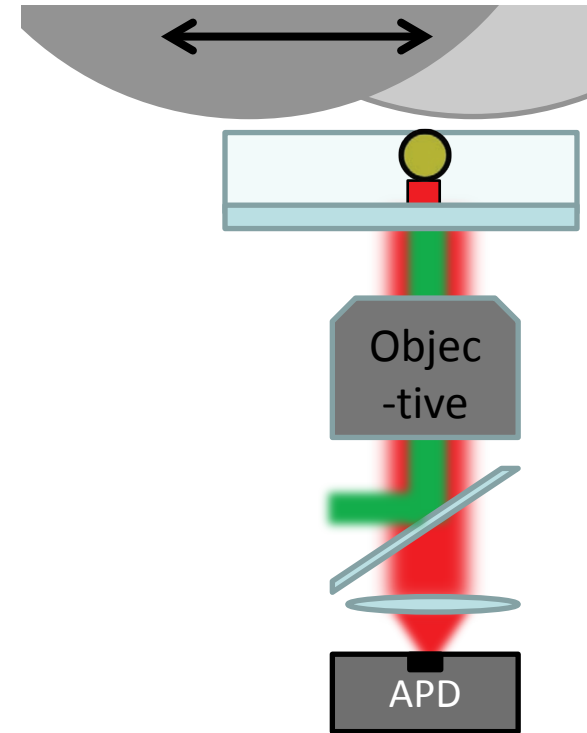
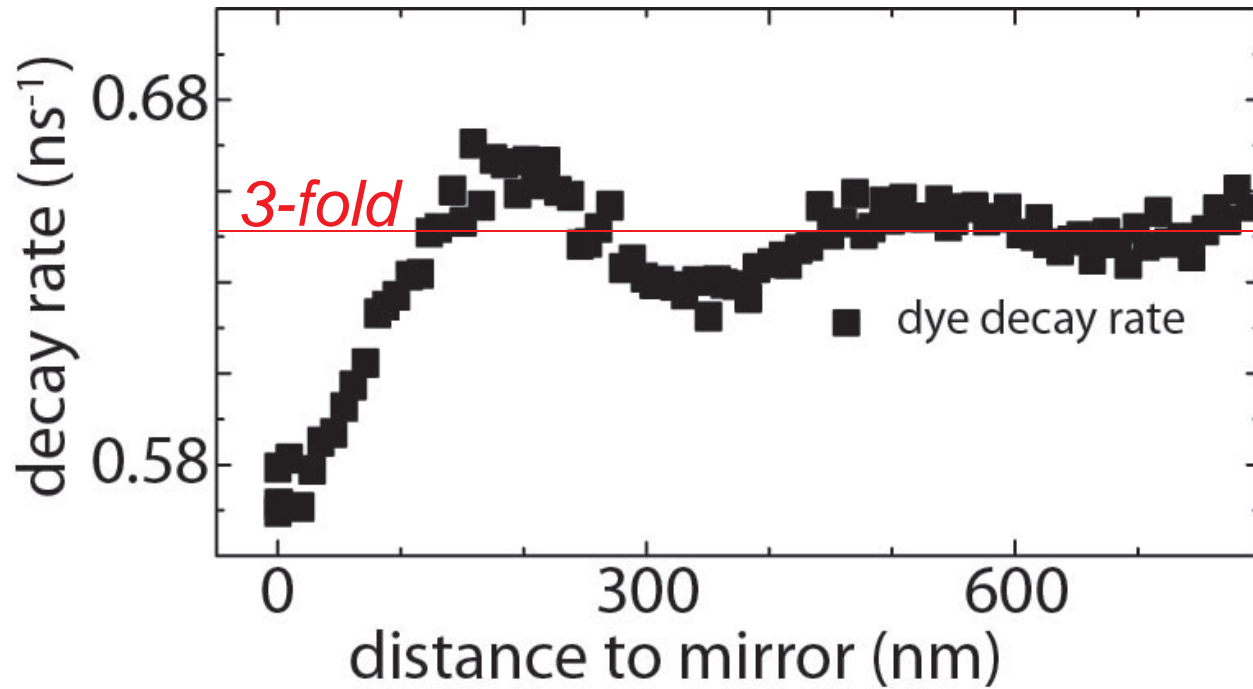


**What happens to the joint radiative impedance, given that I know the radiative impedance change offered by antenna and ground plane ?**

Greffet et al. Phys. Rev. Lett. 105, 117701 (2010) - LDOS as impedance

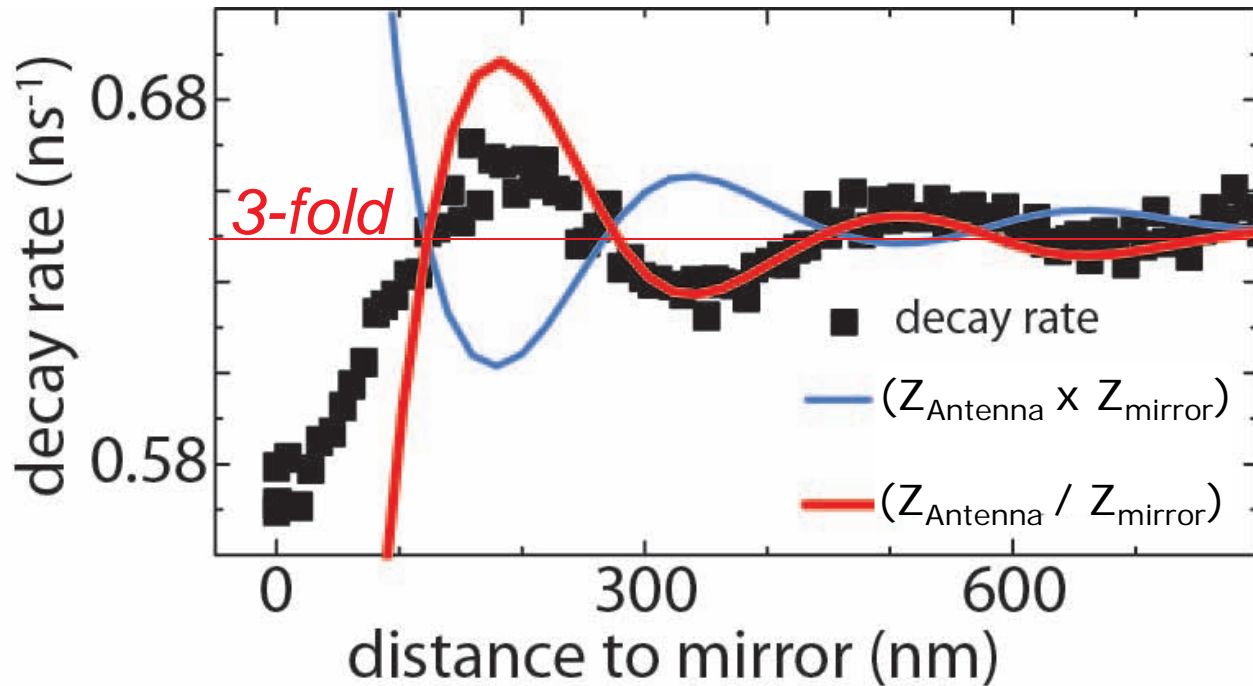
Benson, Nature 480, 193 (2011)

# Scanning mirror 'Drexhage experiment'



Decay rate at superemitter shows characteristic variations  
*Mirror LDOS modifies the already antenna-accelerated decay*

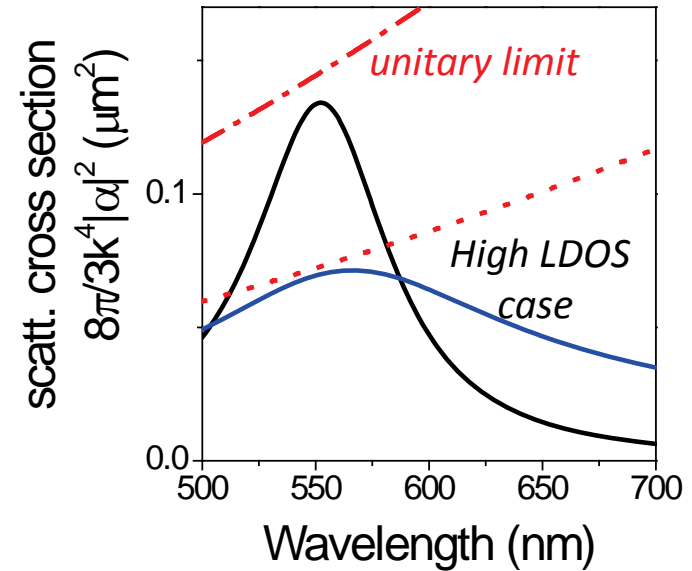
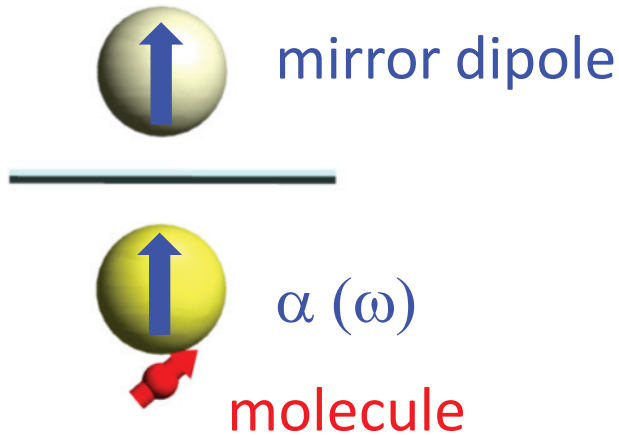
# Scanning mirror 'Drexhage experiment'



Lumped system Purcell factor is clearly not simply a multiplication

**Inverse** effect confirmed by *full* dyadic Green function calculation.

# How an antenna gets spoiled

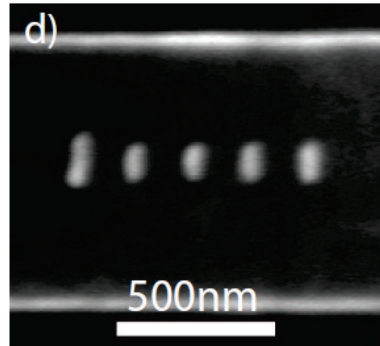


Fixed current sources: twice the dipole moment radiates twice as much  
*quantum emitter: doubled decay rate*

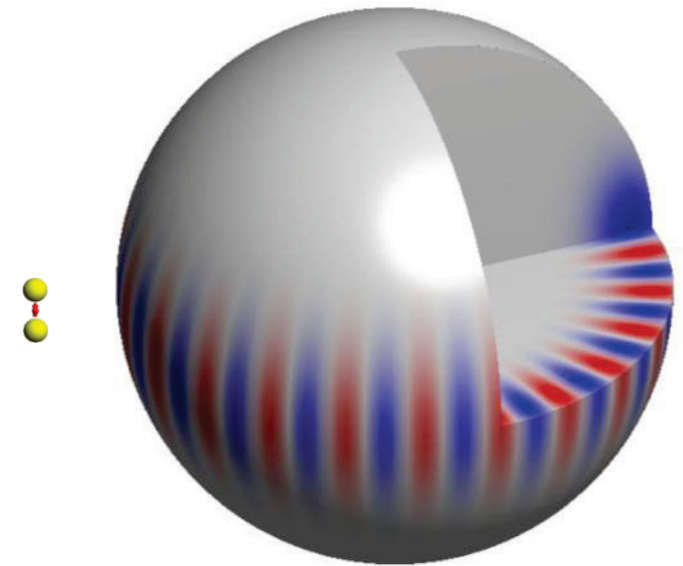
Scatterer: at *twice* the radiative loss, the scatterer  $\mathbf{p}$  is much weaker  
polarizability is *spoiled* / Chu limit changed by the mirror

Theory: Frimmer PRB **86** 235428:1-6 (2012).

# Complex world



Yagi – Uda *ON* a waveguide

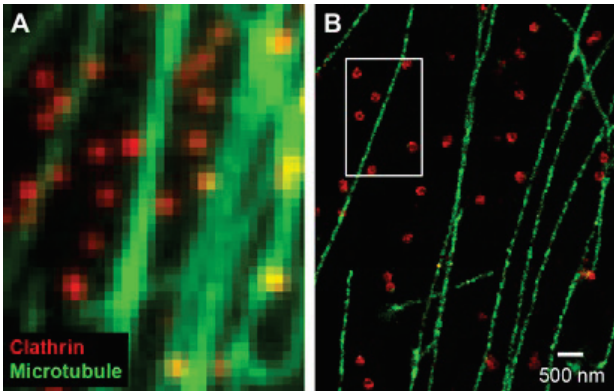


Cavity-assisted plasmonics

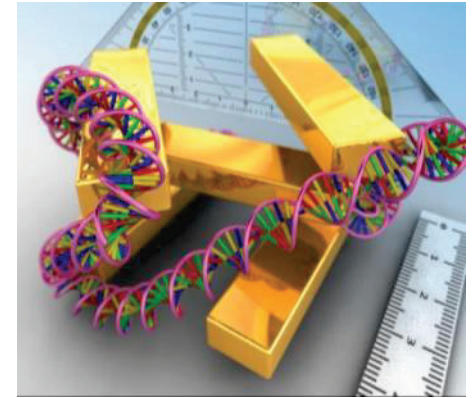
Current effort: *practical*  $Q$ , i.e.,  $Q = 100$ , structures of antenna + cavity  
Separate regimes where cavities aid or spoil antennas

Radiative impedance lumping in complex systems

# Motivation



Bates & Zhuang [PALM, STORM]



Liu & Alivisatos

**Optical microscopy**  
Below  $\lambda/2$  limit

Single molecules  
Information from  
fluctuations

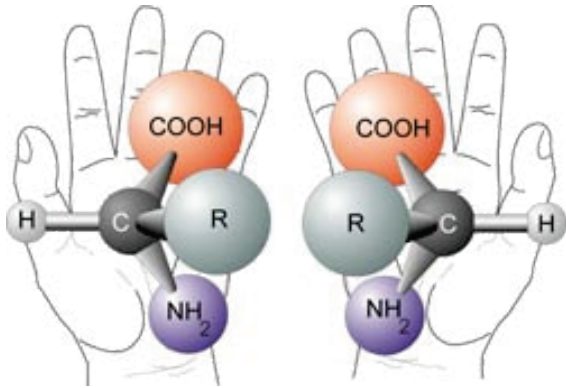
**Single photon sources**  
**Quantum information**  
**Quantum communication**

Quantum information  
in 1 photon can  
**not** be eavesdropped

**Spectroscopy of  
molecules**

Distance ruler  
Vibrations  
THz, IR and VIS

# Handedness



$$\begin{pmatrix} \mathbf{p} \\ \mathbf{m} \end{pmatrix} = \begin{pmatrix} \alpha_E & i\alpha_{EH} \\ -i\alpha_{HE} & \alpha_H \end{pmatrix} \begin{pmatrix} \mathbf{E} \\ \mathbf{H} \end{pmatrix}$$

$$\alpha_E \sim 10^3 \alpha_{EH} \sim 10^6 \alpha_H$$

Almost *only* electrically polarizable

Very weak magnetic moment, induced by electric driving

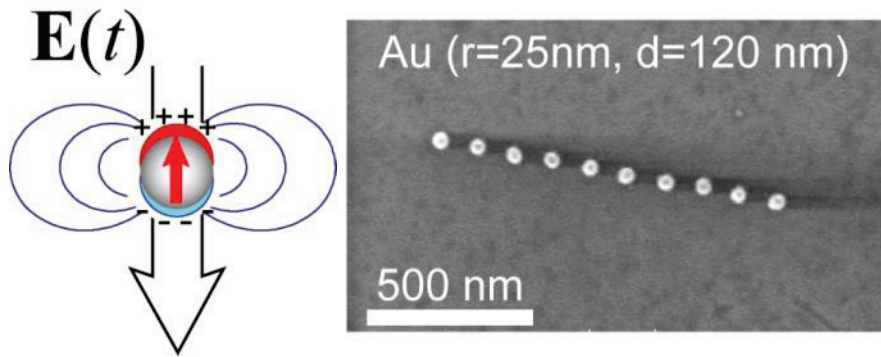
Perturbative effect: optical activity, circular dichroism, optical rotation

Ubiquitous & biochemically of huge impact - optically weak

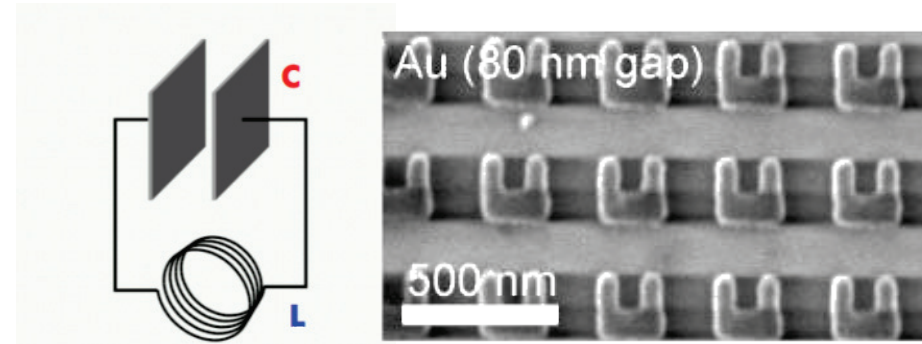


# Resonant nano-scatterers

## Resonant electric dipoles



## Resonant magnetic dipoles



Charge separation: electric dipole moment

Current loop: magnetic dipole moment

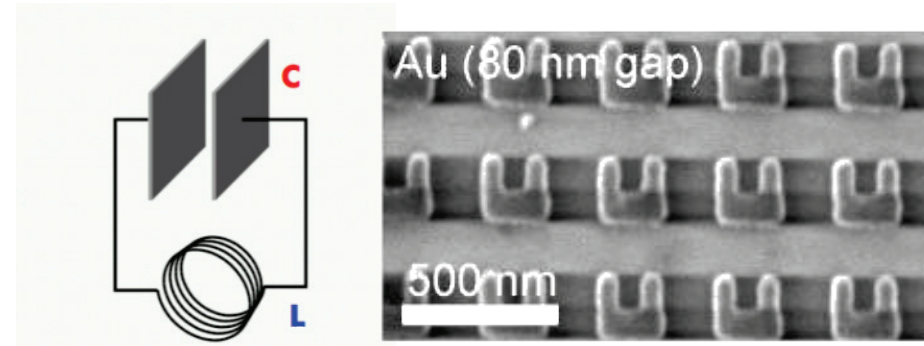
Noble metal U-shaped particles: LC resonators 'split rings'

*Pendry & Smith, Linden & Wegener, Giessen*

Electron beam lithography down to  $20\text{ nm}$  with  $<5\text{ nm}$  error

# Resonant nano-scatterers

$$\begin{pmatrix} \mathbf{p} \\ \mathbf{m} \end{pmatrix} = \begin{pmatrix} \alpha_E & i\alpha_{EH} \\ -i\alpha_{HE} & \alpha_H \end{pmatrix} \begin{pmatrix} \mathbf{E} \\ \mathbf{H} \end{pmatrix}$$



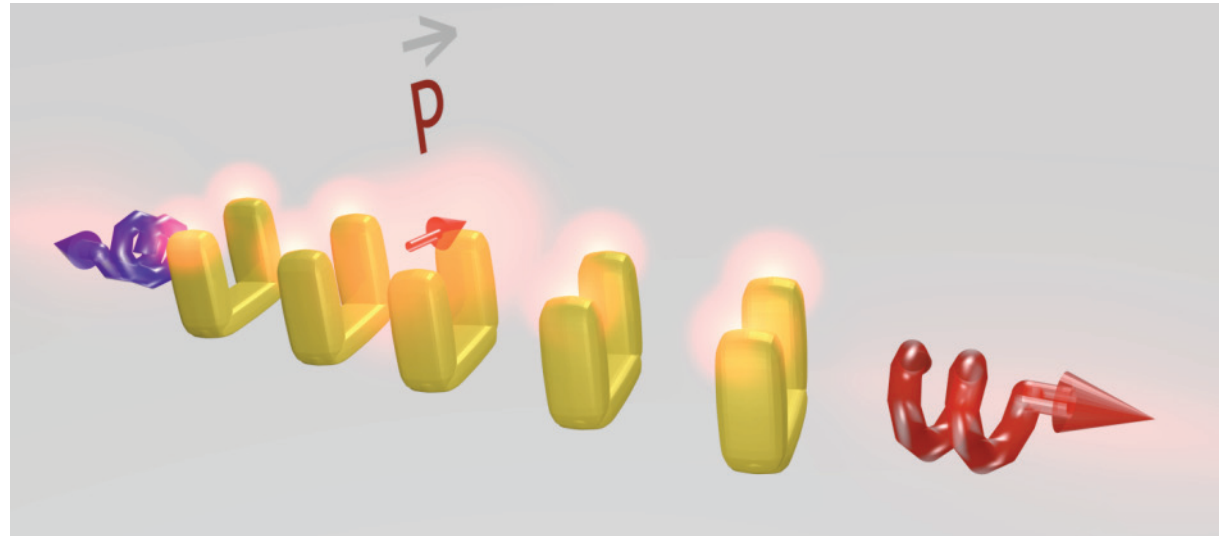
Split ring: E-field charges the split – with a quarter phase lag the split discharges, giving rise to a magnetic dipole

The same polarizability tensor as for chiral molecules, but with

$$\alpha_E \sim \alpha_{EH} \sim \alpha_H \sim V \sim \lambda^3$$

Electron beam lithography down to 20 nm with <5 nm error

# Superchiral spectroscopy

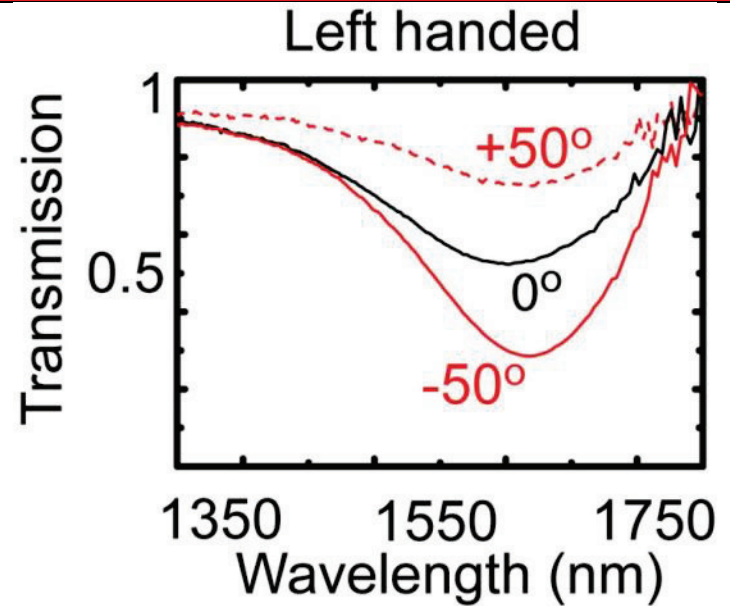
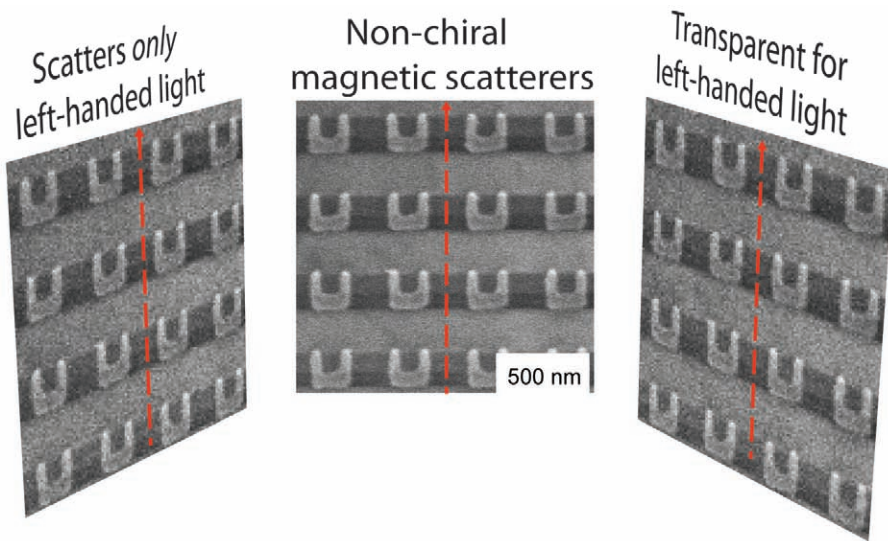


Hendry, Exeter  
Tang & Cohen, Harvard  
Schaferling & Giessen, Stuttgart

Single molecule enantioselective detection ‘superchiral’ fields

Selectively exciting, and spoofing emitters with nontrivial selection rules – spin & orbital angular momentum antennas

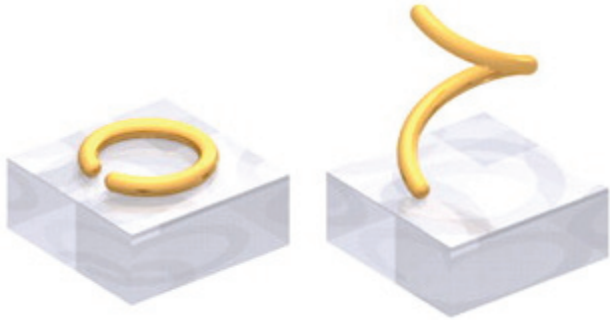
# Not chiral – pseudo chiral



## Pseudochirality

Huge optical activity – though split rings are not chiral at all

# How can an LC circuit / SRR be chiral ?



Geometrically a SRR is not 2D or 3D chiral

Obliquely, the SRR looks like one turn of a screw – COULD be optically active

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Quantitative fit of  $\alpha$  to many angle resolved spectra:

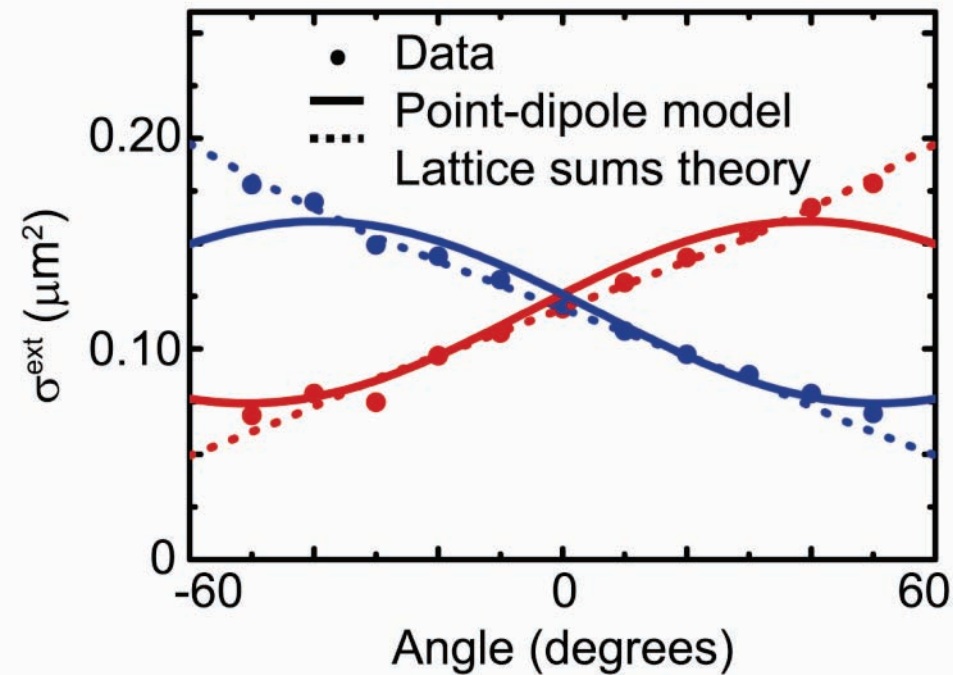
$$|\alpha_E| = 5.7V, |\alpha_H| = 2.3V, |\alpha_C| = 3.4V$$

$$|\alpha_C| \sim 0.88\sqrt{\alpha_E\alpha_H}$$

Strong scattering:  $\alpha$  around 50% of unitary limit  
Hugely optically active or “bi-anisotropic”

Existence of “pseudochirality”: Plum & Zheludev

# Fit of polarizability



Quantitative fit of  $\alpha$  to

$$|\alpha_E| = 5.7V, |\alpha_H| = 2.3V, |\alpha_C| = 3.4V$$

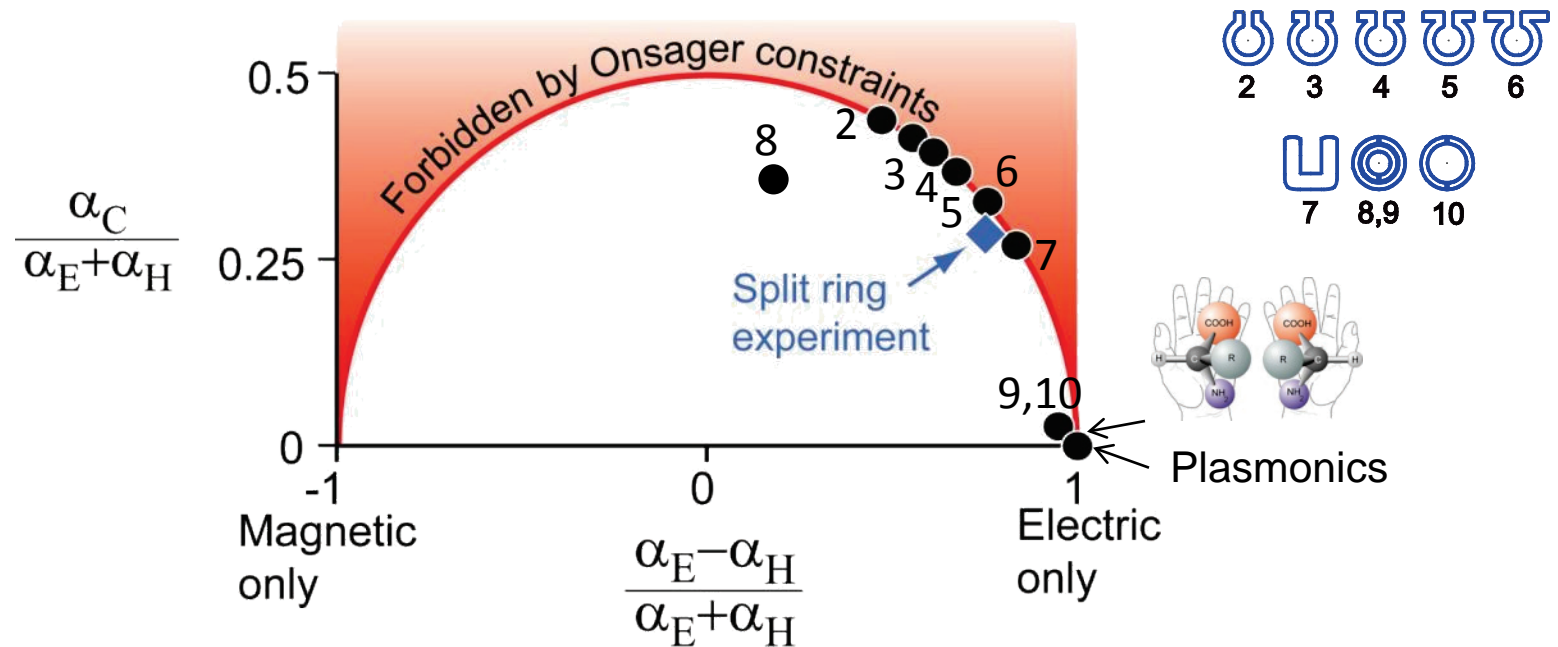
$$|\alpha_C| \sim 0.88\sqrt{\alpha_E\alpha_H}$$

$\alpha$  around 50% of unitary limit

*Strong magnetic scatterers*

*For one handedness, transmission resonance almost disappears entirely*

# Phase diagram



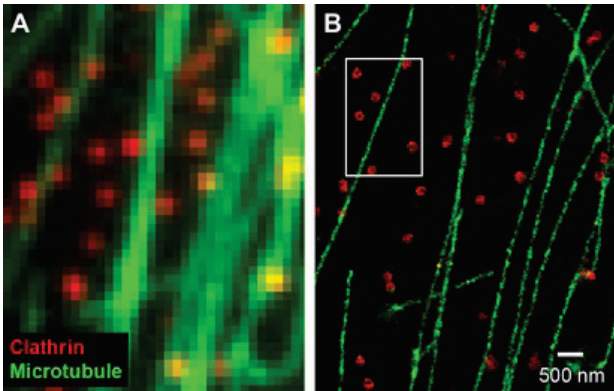
*Almost all meta-scatterers we tested are maximally cross coupled*  
 Reason: free charges generate  $\mathbf{p}$  and  $\mathbf{m}$  – bound by continuity

Method (1):  $\alpha$ -retrieval: Mühlig et al., *Metamaterials* 5, 64 (2011).

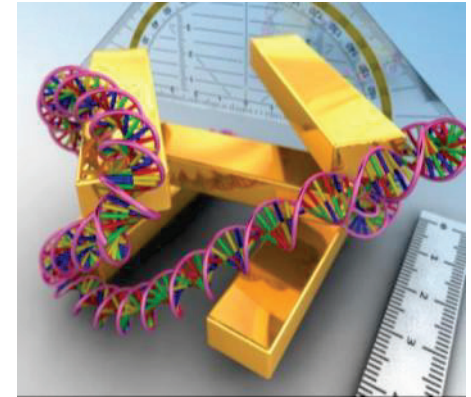
(2): full-field: Kern & Martin, *J. Opt Soc. Am. A* vol. 26, p. 73 (2009)



# Conclusions



Bates & Zhuang [PALM, STORM]



Antenna physics at optical wavelengths:

- Plasmonics instead of perfect metals
- Quantum emitters & single photons instead of  $I$ ,  $V$ ,  $Z$

Phased array physics + radiative impedance + spoof magnetism

Brighter microscopy, quantum optics, spectroscopy & LEDs

# Thanks

## Resonant Nanophotonics AMOLF



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